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Hierarchical Optimal Scheduling Strategy for High Proportion New Energy Power Systems Considering Balanced Response to Grid Flexibility

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ABSTRACT: The penetration rate of new wind and photovoltaic energy in the power system has increased significantly, and the dramatic fluctuation of the net load of the grid has led to a severe lack of flexibility in the regional grid. This paper proposes a hierarchical optimal dispatch strategy for a high proportion of new energy power systems that considers the balanced response of grid flexibility. Firstly, various flexibility resource regulation capabilities on the source-load side are analyzed, and then flexibility demand and flexibility response are matched, and flexibility demand response assessment is proposed; then, a hierarchical optimal dispatch model of the grid taking flexibility adjustment capability into account is established, and the upper model optimizes the net load curve with the objectives of minimizing the fluctuation of the net load, maximizing the benefits of energy storage and controllable loads, and optimizing the flexibility adjustment capability. The upper layer model optimizes the net load curve by minimizing net load fluctuation, maximizing energy storage and controllable load revenue, and optimizing flexibility adjustment capability. In contrast, the lower layer model optimizes the power allocation of thermal power units and regulates the lost load of wind and solar power generation by minimizing the total system operating cost. The results show that the proposed strategy improves the flexibility of the grid by 15.2%, gives full play to the regulation capability of each flexibility resource, and reduces the fluctuation of the net load by 15.6% to achieve optimal coordination between different types of flexibility resources.

KEYWORDS: Flexibility; demand response; regulatory capacity; equilibrium; economic dispatch

1 Introduction

With China's 'dual-carbon' goal [1–3], the penetration of new energy sources has been increasing and has become an integral part of the power system. However, this also exacerbates the randomness and volatility of power grid operations [4–7]. As the proportion of new energy continues to rise, it is crucial to explore how to utilize different types of energy to complement one another to reduce the abandonment of wind and photovoltaic power and enhance the overall flexibility of the power grid. This presents an urgent problem that must be addressed. In traditional grid scheduling and control, new energy sources operate in conjunction with the grid but do not participate in active control, resulting in a significant shortage of regulated resource capacity at the receiving end of the grid [8–11]. As net load fluctuations increase, many optimal scheduling strategies struggle to achieve timely balanced regulation of flexibility resources since grid scheduling primarily prioritizes the economic operation of the system [12–15]. This focus complicates the ability to ensure adequate flexibility and diminishes the grid's resilience to risks.



In terms of grid flexibility [16–19], domestic and international studies primarily focus on the power side and the grid side, with numerous investigations dedicated to assessing flexibility resources [20,21]. One study presents a day-ahead scheduling method for renewable energy systems that balances flexibility and economy [22]. This study proposes a new Integrated Resource Strategic Planning Framework for Interregional Flexibility (IRSP-IF) that assesses cross-regional flexibility needs and optimizes cross-regional power resource allocation [23]. In the paper, an optimization strategy for flexible operation is proposed at the system level to guide the real-time flexible ramping of the grid, and a ramping factor is proposed as a flexibility metric, which focuses more on flexibility than on economics compared to the traditional model [24]. Combining the advantages of the capacity expansion model SWITCH-China and the production simulation model PLEXOS, this study analyses the flexibility options for China's renewable energy-dominated power system under different Scenarios and finds that a larger balancing area can lead to direct flexibility advantages [25]. One study presents a comprehensive three-phase framework for unlocking the flexibility capabilities of energy communities and microgrids in balancing markets, aiming to eliminate real-time imbalances between energy production and consumption [26]. One study proposes a new methodology to assess the flexibility of DC renewable energy systems when covering regional lines. It introduces a new quantitative metric called the Flexibility Deployment Index (FDI) [27].

To enhance the balanced regulation of flexible resources over time, extensive research has been conducted on optimal scheduling strategies for energy management [28]. Key studies have focused on optimizing the use of regional energy sources with an emphasis on flexibility and reliability [29–31]. A study proposes an energy storage behavioral decision-making model based on the Soft Behavioural Critique (SAC) algorithm for energy storage system (ESS) scheduling, and by analyzing the output characteristics of wind farms, the output of the wind power prediction model can be used as a wind farm scheduling plan [32]. The study proposes an integrated energy system configuration and optimal scheduling method for hydrogen-to-ammonia and ammonia-mixed-oxygen-enriched combustion in thermal power units, which enriches the system products and improves the economic efficiency through the introduction of an ammonia synthesis system [33]. This study uses a two-stage optimization technique to solve the problem of optimal location and sizing of battery energy storage (BES) devices [34]. This study proposes an optimal scheduling strategy for ES-MCS under the Integrated Carbon Green Certificate Trading (ICGCT) mechanism to further reduce the carbon emission level of the Energy Storage-Multiple Complementary System (ES-MCS) and to improve the economics of the system operation [35]. This study proposes a three-objective scheduling strategy for island microgrids based on the Improved Multi-Objective Particle Swarm Optimisation (IMOPSO) algorithm, which considers the economic cost, renewable energy utilization, and user satisfaction [36]. A study models stochastic electric utility outages caused by flooding and develops appropriate power system dispatch strategies for extreme precipitation events [37]. This study proposes an electricity-steam-based coordinated optimal scheduling method for virtual power plants to effectively address the challenges of customer load regulation in the textile industry [38]. The article presents an innovative active and reactive power optimal dispatch model to maximize community welfare [39]. This article presents a Membrane Search Algorithm (MSA) based on the theory of membrane computation, which is improved for the problem of minimizing ORPD transmission losses in complex, non-convex, non-linear, and discrete power systems [40]. This study describes a framework for multiple incentives for PEDF parks, a type of building energy system that employs PEDF technology, and the proposed incentives include both economic and non-economic aspects [41]. Lastly, a unique characterization method [42] is proposed, featuring a learning module and an updating module. This approach tackles the challenges posed by conventional methods when managing AC currents and numerous Renewable Distributed Energy Resources (RDERs), providing a more accurate evaluation.

The existing literature extensively evaluates various flexibility resources and suggests effective methods. However, these studies primarily focus on assessing flexibility supply capacity, often overlooking the crucial aspect of matching supply with demand. The full potential of user-side resources remains untapped, highlighting the need for advanced modeling and control techniques to represent user behavior in demand response Scenarios accurately. Furthermore, current research rarely considers the integrated use of multiple flexibility resource types, which can complement each other. This oversight hinders the efficient utilization of all available resources within the grid. To address these gaps, a more holistic approach is essential for optimizing grid resource management.

In summary, this paper proposes a hierarchical optimal scheduling strategy for high-ratio new energy power systems that considers the balanced response of grid flexibility. The details are as follows: first, the regulation capabilities of various flexibility resources on the source-load side are analyzed, and then the flexibility demand/response module is established to determine the flexibility resources and their constraints involved in dispatch at each period by calculating the matching results during the demand response dispatch cycle. Then, a two-layer optimization is used, where the upper model takes the minimum net load fluctuation, the maximum benefit of storage and controllable load, and the optimal flexibility adjustment capability as the objectives and considers the storage and controllable load constraints to optimize the net load curve. The lower model takes the minimum total operating cost as the objective and considers the thermal constraints, power balance constraints and so on to enable the thermal units to allocate power. Finally, simulation verification through the arithmetic system shows that the scheduling strategy improves the flexibility of the grid and promotes the coordination between flexible resources while considering the economy.

This paper's innovations are as follows: it matches the supply and demand of grid flexibility, which improves the applicability of flexibility resources to the grid; it actively uses load-side resources to participate in scheduling, which increases the scheduling range and improves the economy of system operation; and it adopts a two-layer optimization model, which takes into account the temporal equilibrium of grid flexibility.

2 Source-Load Side Adjustable Resource Capacity Analysis and Scheduling Strategy Framework

2.1 Source-Load Side Adjustable Resource Capacity Analysis

This paper explores diverse adjustable resources within the regional power grid, including new energy stations, thermal power plants, pumped storage facilities, energy storage sites, and controllable loads. As illustrated in Fig. 1, these resources face challenges due to the high volatility of net load. This results in the underutilization of flexibility resource capacity on the source-load side. Additionally, the load side comprises various flexibility resources, hindering the development of large-scale flexibility regulation resources.

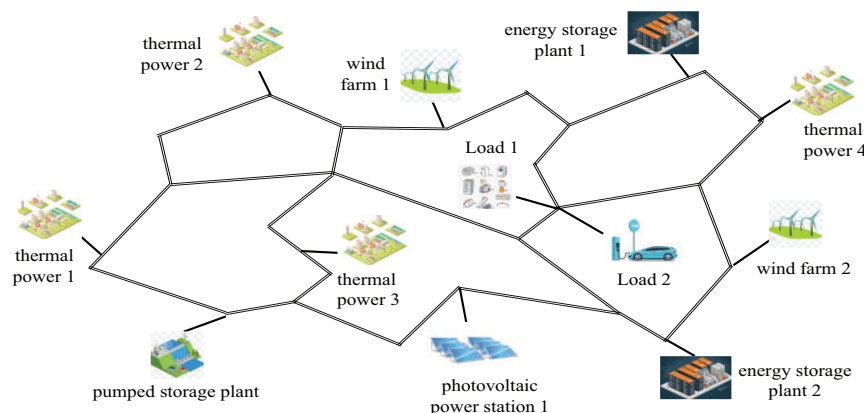


Figure 1: Schematic of a regional grid with multiple flexibility resources

The regional power grids boast diverse flexibility resources, integrating numerous distributed power sources, various energy storage solutions, and different types of loads. These resources are characterized by their uncertainty and decentralization. To effectively enhance the capability of regional power grids to handle unpredictability, achieving an optimal balance between supply and demand is essential. This optimization enhances the grid system's economic, temporal, and spatial attributes. Flexibility resources are primarily located on both the power supply and load sides. The power supply side includes thermal power units, hydropower units, wind power units, photovoltaic systems, pumped storage power stations, and various energy storage facilities. On the load side, flexibility is provided by curtailable loads, transferable loads, and several energy storage technologies. Conventional units, renewable energy sources, diverse energy storage systems, and controllable loads form the backbone of the regional power grid's flexibility resources, ensuring improved grid reliability and efficiency.

Traditional energy units offer upward and downward flexibility by increasing or decreasing their output in the realm of flexibility resources. On the other hand, renewable energy sources, such as wind and solar power, provide downward flexibility by occasionally curtailing wind or light usage. The capabilities for adjusting this flexibility, both upward and downward, are detailed in Eqs. (1) and (2) [43].

$$\begin{cases} P_{g,i,t}^{\text{up}} = \min \{ P_{g,i,t-1} + \Delta P_{g,i}^{\text{up}}, P_{g,i}^{\text{max}} \} \\ P_{g,i,t}^{\text{down}} = \max \{ P_{g,i,t-1} - \Delta P_{g,i}^{\text{down}}, P_{g,i}^{\text{min}} \} \end{cases} \quad (1)$$

$$\begin{cases} P_{w,j,t}^{\text{up}} = P_{w,j,t}^{\text{max}} \\ P_{pv,k,t}^{\text{up}} = P_{pv,k,t}^{\text{max}} \\ P_{w,j,t}^{\text{down}} = P_{pv,k,t}^{\text{down}} = 0 \end{cases} \quad (2)$$

Style: $P_{g,i,t}^{\text{up}}, P_{g,i,t}^{\text{down}}$ consists of t upward and downward flexibility of the i th conventional unit in period; $P_{g,i}^{\text{max}}, P_{g,i}^{\text{min}}$ is the maximum and minimum output of the i th conventional unit; $P_{g,i,t-1}$ is the output of the i th conventional unit in period $t-1$; $\Delta P_{g,i}^{\text{up}}, \Delta P_{g,i}^{\text{down}}$ is the upward as well as downward climbing capacity of the i th conventional unit; $P_{w,j,t}^{\text{up}}, P_{w,j,t}^{\text{down}}$ are the upward and downward flexibility adjustments of the j th wind turbine in period t ; $P_{pv,k,t}^{\text{up}}, P_{pv,k,t}^{\text{down}}$ are the upward and downward flexibility adjustment capacities of the k th PV at time t ; $P_{w,j,t}^{\text{max}}$ is the maximum output power of the j th wind turbine in period t ; $P_{pv,k,t}^{\text{max}}$ is the maximum output power of the k th PV in period t .

Electrochemical energy storage systems and pumped storage solutions both excel in offering upward and downward flexibility regulation. These methods are recognized as highly regulated flexibility resources, as demonstrated in Eq. (3) [43].

$$\begin{cases} P_{b,h,t}^{\text{up}} = \min \{ P_{b,h}^{\text{n}}, (E_{b,h,t} - E_{b,h}^{\text{min}}) \cdot \eta_h / t \} \\ P_{b,h,t}^{\text{down}} = \max \{ -P_{b,h}^{\text{n}}, (E_{b,h,t} - E_{b,h}^{\text{max}}) / \eta_h / t \} \end{cases} \quad (3)$$

Style: $P_{b,h,t}^{\text{up}}, P_{b,h,t}^{\text{down}}$ are the maximum and minimum flexibility output power of the h th energy storage device at time t , respectively; $P_{b,h}^{\text{n}}$ is the rated power of the h th energy storage device in the power system; $E_{b,h,t}$ is the energy of the h th energy storage device in period t ; $E_{b,h}^{\text{max}}, E_{b,h}^{\text{min}}, \eta_h$ are energy upper and lower limits and efficiency of the h th energy storage unit.

Controllable loads offer significant flexibility in energy management by allowing the adjustment of power usage. Switching loads on or off can effectively increase upward and downward regulation capabilities.

This makes them an excellent resource for enhancing system flexibility while delivering substantial benefits. Eq. (4) [43] demonstrates the ability to manage power demand efficiently through controllable loads.

$$\begin{cases} P_{cl,m,t}^{\text{up}} = \min \{ P_{cl,m}^{\text{max}}, (P_{cl,m,t-1} + \Delta P_{cl,m}^{\text{max}}) \} \\ P_{cl,m,t}^{\text{down}} = \max \{ 0, (P_{cl,m,t-1} - \Delta P_{cl,m}^{\text{min}}) \} \end{cases} \quad (4)$$

Style: $P_{cl,m,t}^{\text{up}}$, $P_{cl,m,t}^{\text{down}}$ is the upward and downward flexibility of the m th interruptible load in period t ; $P_{cl,m}^{\text{max}}$ is the maximum power of the m th interruptible load; $P_{cl,m,t-1}$ is the power of the m th interruptible load in period $t-1$; $\Delta P_{cl,m}^{\text{max}}$, $\Delta P_{cl,m}^{\text{min}}$ is the maximum increase and decrease the power of the m th interruptible load.

This subsection comprehensively evaluates the flexibility resources available within the regional grid. It identifies the grid's capacity for flexibility adjustments, crucial for conducting future flexibility demand response assessments. This evaluation helps lay the groundwork for practical regional flexibility demand response analysis.

2.2 Scheduling Strategy Framework

This paper introduces a hierarchical optimal scheduling strategy to enhance the cost and performance of flexible resources in new energy power systems, such as thermal power units and energy storage plants. By focusing on both the source and load sides, our approach seeks to achieve a balanced response in grid flexibility. Initially, the strategy involves a comprehensive data collection process that assesses the flexibility of demand response. This assessment gathers crucial information, including new energy output data, load data, and parameters of flexibility resources. These insights then match the flexibility demand with the flexibility adjustment capacity. Furthermore, we identify the power and start-stop constraints of flexibility resources, which are incorporated into a grid hierarchical optimal dispatch model, emphasizing flexibility adjustment capacity. The model operates through two key layers: the power allocation layer and the total operating cost optimization layer. Together, they deliver optimized scheduling results, ensuring efficient power distribution and minimized operational costs. For a detailed overview of the framework, please refer to Fig. 2. By implementing this strategy, power systems can significantly improve flexibility and cost-efficiency, ultimately leading to more sustainable energy management.

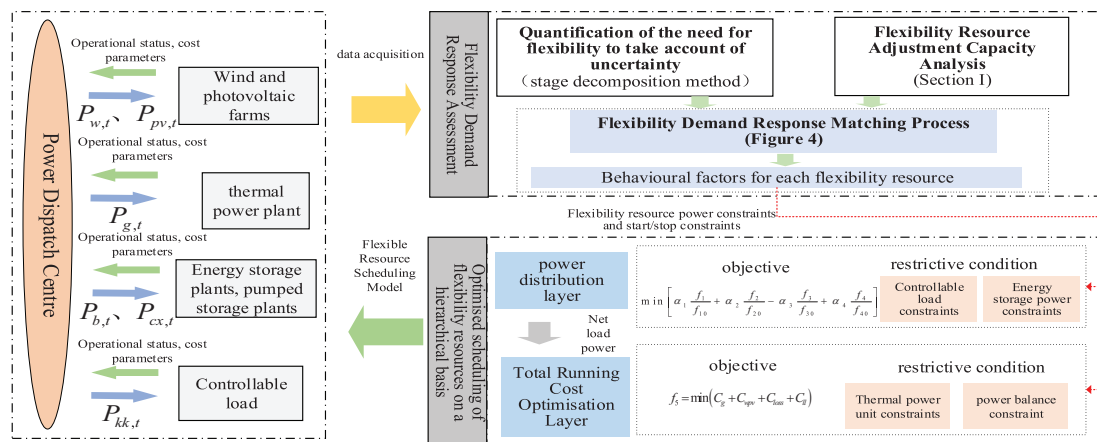


Figure 2: Block diagram of hierarchical optimal dispatch strategy for multi-energy systems considering balanced response to grid flexibility

3 Flexibility Demand Response Assessment

Fig. 3 illustrates the framework for aligning flexibility needs with appropriate responses. This process primarily involves aligning decomposed flexibility demand analyses with the capabilities of flexibility resources. To begin with, a flexibility demand quantification method calculates the range of flexibility needs. Next, a stage decomposition method identifies the extreme points on the flexibility demand curve. By integrating and differentiating the curve between these points, the total flexibility demand for this stage is determined. Incorporating keywords seamlessly into your content will enhance its visibility to your target audience. $S_{i,xq}$ and climb demand at time t $P_{i,xq}^t$. Flexibility regulating capacity is then analysed using the methodology in Section 1 to obtain an upper limit on the total amount of flexibility resources to be regulated $S_{i,max}$ and the upper and lower limits of flexibility resource creep in period t . $P_{i,max}^t$, $P_{i,min}^t$. In conclusion, we assess how well each type of flexibility resource aligns with the total flexibility demand and the specific demands related to climbing characteristics. This evaluation ensures optimal resource allocation and performance.

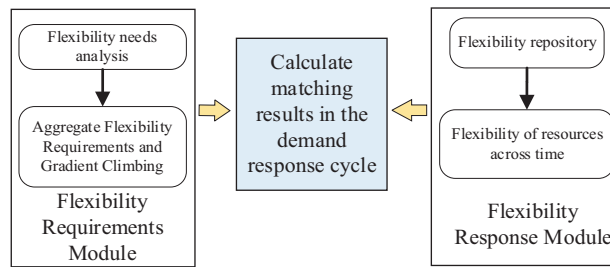


Figure 3: Flexible demand response matching framework

To accurately assess the total flexibility demand and the climb demand for each period, it is essential to consider the dynamic range of flexibility phases. This can be achieved by integrating and differentiating the flexibility curves. Understanding these phases can provide deeper insights into meeting flexibility demands effectively. Fulfill a condition $S_{i,xq} \leq S_{i,max}$ and $P_{i,min}^t \leq P_{i,xq}^t \leq P_{i,max}^t$, if the fulfilment of the $P_{i,xq}^t \geq 0$, the priorities for flexibility resources to participate in dispatch are thermal power, pumped storage, storage, and low-capacity pumped storage and storage; If the fulfilment of the $P_{i,xq}^t \leq 0$, the priorities for flexibility resources to participate in dispatch are controllable loads and thermal power, pumped storage, energy storage, and high-capacity pumped storage and energy storage; Fulfil a condition $S_{i,xq} \geq S_{i,max}$ and $P_{i,min}^t \leq P_{i,xq}^t \leq P_{i,max}^t$, if the fulfilment of the $P_{i,xq}^t \geq 0$, the order of priority for flexibility resources to participate in dispatch is thermal power, pumped storage, and energy storage; if the fulfilment of the $P_{i,xq}^t \leq 0$, the priorities for flexibility resources to participate in dispatch are controllable loads and thermal power, pumped storage, and energy storage; Otherwise, flexibility resources are fully involved in dispatch and are considered for grid dispatch for wind, light and load loss.

In this phase, the limitations of flexibility resources are determined based on their roles in scheduling priorities. This includes constraints related to power balance and equipment output. As outlined in Eq. (5), at any given time (t), the output power of flexibility resources must meet the specified modal power demand. Additionally, the maximum output power for each type of flexibility resource at time (t) is detailed in Section 2.1.

$$P_{load,t} = \mu_1 P_{g,t} + \mu_2 P_{w,t} + \mu_3 P_{pv,t} + \mu_4 P_{b,t} + \mu_5 P_{cx,t} - \mu_6 P_{kk,t} + \mu_{loss} P_{loss,t} \quad (5)$$

Style: $P_{load,t}$ is the load power at time period t ; $P_{g,t}$, $P_{w,t}$, $P_{pv,t}$, $P_{b,t}$, $P_{cx,t}$ and $P_{kk,t}$ is the thermal power output, wind power, photovoltaic power, energy storage power, pumped storage power and controllable load power in time period t ; μ_{1-6} as behavioural factors for each flexibility resource. $\mu_1 = 1$ indicates that thermal power is involved in this phase of the scheduling process. $\mu_1 = 0$ indicates that thermal power is not involved in this phase of the scheduling process; $P_{loss,t}$ is the lost load power at period t ; μ_{loss} for the behavioural factor of loss of load. $\mu_{loss} = 1$ Indicating that the demand for flexibility is greater than the capacity to reconcile resources for flexibility. Conversely, $\mu_{qs} = 0$ illustrates the balance between supply and demand for flexibility.

Finally, the overall flexibility demand response matching process is shown in Fig. 4.

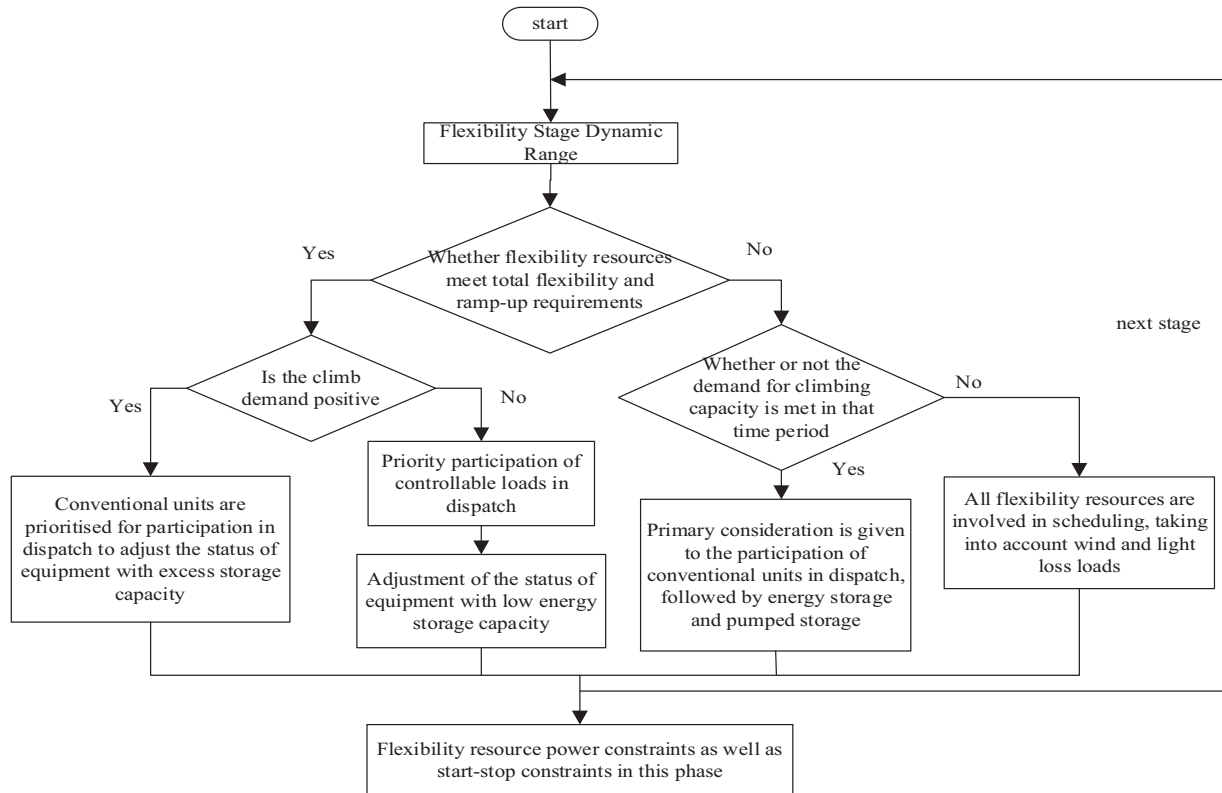


Figure 4: Flexibility demand response matching process

4 A Hierarchical Optimal Dispatch Model for Power Grids with Flexibility Adjustment Capability

Economic management is crucial for optimizing flexibility resource aggregation in the electrical grid, with balance playing an essential role. Flexibility resource aggregation involves mapping the adjustable power range of a grid's flexibility resources to the nodes connecting regional grids to a larger grid, all while considering network and equipment constraints. By consolidating dispersed resources, grid scheduling becomes more flexible and precise, enhancing overall system efficiency. However, promptly balancing flexibility regulation capabilities can lead to security risks. To ensure timely and balanced flexibility, regulation, scheduling, and safety must be prioritized in this aggregation process. This paper suggests a hierarchical optimal dispatch model designed explicitly for regional grids to enhance grid efficiency and reliability, incorporating flexibility adjustment capacity.

In this study, we quantify grid flexibility and develop a hierarchical optimal dispatch model by leveraging flexibility from both the energy source and load perspectives. The upper-level model is designed with

several key objectives: minimizing net load fluctuations, reducing operating costs for pumped and energy storage, maximizing controllable load benefits, and optimizing flexibility adjustment capabilities. This model prioritizes the adjustment of power from energy and pumped storage, and it forwards the residual power and output from identified flexibility resources to the lower-level model. The lower-level model aims to minimize costs associated with thermal power operation, wind and solar curtailment, and loss-of-load penalties. It also considers constraints related to thermal power unit operations, power balance, contact line power limits, and operational security. The dispatch model aims to enhance grid efficiency and reduce costs by addressing these objectives and constraints.

4.1 Upper Level Model

4.1.1 Objective Function

The primary goal of the upper-level model is to achieve the following: minimize net load fluctuations, reduce operating costs associated with pumped storage, maximize gains from controllable loads, and optimize flexibility adjustment capabilities. This is accomplished using the following formulae:

$$f_1 = \min \frac{1}{T} \sum_{t=1}^T \left[\left(P_{load,t} - P_{b,t}^{\text{dis}} + P_{b,t}^{\text{ch}} - P_{cx,t}^{\text{dis}} + P_{cx,t}^{\text{ch}} - P_{pv,t} - P_{w,t} - P_t^{\text{jl}} \right) \right]^2 \quad (6)$$

$$P_t^{\text{jl}} = \frac{1}{T} \sum_{t=1}^T \left(P_{load,t} - P_{b,t}^{\text{dis}} + P_{b,t}^{\text{ch}} - P_{cx,t}^{\text{dis}} + P_{cx,t}^{\text{ch}} - P_{w,t} - P_{pv,t} \right) \quad (7)$$

$$f_2 = \min (C_b + C_{cx}) \quad (8)$$

$$f_3 = \max C_{kkfh} \quad (9)$$

$$f_4 = \min \frac{H_{bd}}{H_{fw}} \quad (10)$$

Style: f_1, f_2, f_3, f_4 are the four subfunctions of the objective function; T is the total number of times in the scheduling cycle; $P_{b,t}^{\text{ch}}, P_{b,t}^{\text{dis}}$ is the charging and discharging power of the stored energy at time period t ; $P_{cx,t}^{\text{ch}}, P_{cx,t}^{\text{dis}}$ is the charging and discharging power of pumped storage at time t ; P_t^{jl} is the average net load during the dispatch cycle; C_b, C_{cx} for the operating costs of energy storage vs. pumped storage; C_{kkfh} for the gain of controllable loads; H_{bd} is the degree of flexibility equilibrium; H_{fw} is flexibility dynamic range.

To begin with, the four objective functions undergo normalization. Significant adjustments in the net load fluctuation weight coefficients can impact the economic efficiency of energy storage and controllable loads. This section evaluates the flexibility requirements at each stage to determine the optimal net load fluctuation weights and achieve a balanced system that prioritizes economy and flexibility. As a result, it derives various weight coefficients. Consequently, the refined objective function is:

$$\min \left[\alpha_1 \frac{f_1}{f_{10}} + \alpha_2 \frac{f_2}{f_{20}} - \alpha_3 \frac{f_3}{f_{30}} + \alpha_4 \frac{f_4}{f_{40}} \right] \quad (11)$$

$$\alpha_1 = 0.1e^{\varepsilon_1} \quad (12)$$

$$\alpha_2 = 0.2\varepsilon_2 \quad (13)$$

$$\alpha_3 = 0.2(1 - \varepsilon_2) \quad (14)$$

$$\alpha_4 = 1 - \alpha_1 - \alpha_2 - \alpha_3 \quad (15)$$

$$\varepsilon_1 = \frac{T \sum_{t=1}^{T_i} J_t}{T_i \sum_{t=1}^{T_i} J_t} \quad (16)$$

$$J_t = \left| P_{load,t} - P_{load,t+1} + P_{d,t+1}^{fw} - P_{d,t}^{fw} + P_{d,t+1}^{fpv} - P_{d,t}^{fpv} \right| \quad (17)$$

$$\varepsilon_2 = \frac{10 \sum_{t=1}^{T_i} \frac{P_{load,t+1} - P_{load,t}}{P_{load,t}}}{T_i} \quad (18)$$

Style: $\alpha_1, \alpha_2, \alpha_3, \alpha_4$ are the weight coefficients corresponding to the four sub-objective functions. f_{10} is the reference quantity for Sub-Objective 1 and is the net load variance at the time of low valley electricity consumption; f_{20} The reference quantity for Sub-Objective 2 is the operating cost during low valley electricity consumption; f_{30} The reference quantity for sub-goal 3 is the gain under low valley electricity consumption; f_{40} The reference quantity for sub-goal 4 is the flexibility adjustment capacity under low valley electricity consumption; $\varepsilon_1, \varepsilon_2$ is the dynamisation factor; J_t is the fluctuating power at time period t ; T_i is the i th phase cycle; $P_{d,t}^{fw}, P_{d,t}^{fpv}$ is the predicted output power of wind farms and PV plants in the t th time period.

4.1.2 Upper Level Model Constraints

(1) Energy storage and pumped storage constraints

Since pumped storage can also be regarded as energy storage, their constraints are basically the same, with the following equations [44].

① Energy storage charge/discharge constraints

$$\mu_{m,t}^d + \mu_{m,t}^c \leq 1 \quad (19)$$

Style: $\mu_{m,t}^{d/c}$ denotes the discharging as well as charging state of the m th energy storage in time period t . It is 1 when it is working and 0 otherwise.

② Charge state constraints

$$S_{\min} \leq S_{m,t} \leq S_{\max} \quad (20)$$

$$|S_{m,1} - S_{m,t}| \leq \Delta S_{m,\max} \quad (21)$$

$$S_{m,t+1} = S_{m,t} + \left(\eta_m P_{b,m,t}^c - \frac{P_{b,m,t}^d}{\eta_m} \right) \Delta t / E_{m,N} \quad (22)$$

Style: S_{\min}, S_{\max} are the upper and lower limits of the charge state; $S_{m,t}$ is the charging state of the m th energy storage at time period t ; $\Delta S_{m,\max}$ is the maximum range of change in SOC for the m th energy storage at the beginning and end of the scheduling cycle; $P_{b,m,t}^c, P_{b,m,t}^d$ is the charging and discharging power of the m th energy storage in time period t ; η_m is the charging and discharging efficiency of the m th energy storage; Δt for the unit time period; $E_{m,N}$ is the rated capacity of the m th energy storage.

③ Charge and discharge power constraints

$$0 \leq \mu_{m,t}^{d/c} P_{b,m,t}^{d/c} \leq P_{m,N} \quad (23)$$

Style: $P_{m,N}$ is the rated power of the m th energy storage.

(2) Controllable load constraints [45]

$$P_{min,z}^{cl} \leq P_{z,t}^{cl} \leq P_{max,z}^{cl} \quad (24)$$

$$\sum_{t=1}^T (1 - v_{z,t-1}) v_{z,t} \leq N_{max}^{cl} \quad (25)$$

Style: $P_{max,z}^{cl}$, $P_{min,z}^{cl}$ are the upper and lower limits of controllable load interruption capacity at node z , respectively; $P_{z,t}^{cl}$ is the interrupt capacity of the controllable load at node z ; $v_{z,t}$ is the state variable of the controllable load at node z in time period t , which is 1 for turn-on and 0 for turn-off; N_{max}^{cl} is the maximum number of interrupts.

4.2 Lower Level Model

4.2.1 Objective Function

The objective function is to minimize the total operating cost, excluding energy storage and controllable loads f_5 . This includes the cost of wind O&M, the cost of running conventional thermal power, the cost of wind and light abandonment, and the cost of lost load penalties, with the following formula:

$$f_5 = \min (C_g + C_{wpv} + C_{loss} + C_{ll}) \quad (26)$$

$$C_g = \sum_{t=1}^T a P_{g,t}^2 + b P_{g,t} + c + e^{on} D_{g,t} + e^{off} D_{g,t} \quad (27)$$

$$C_{wpv} = \lambda_{wind} P_{w,t} + \lambda_{pv} P_{pv,t} \quad (28)$$

$$C_{loss} = c_{loss}^{wind} \left(\sum_{t=1}^T P_{loss,t}^{wind} - \sum_{t=1}^T 0.05 P_{w,t} \right) + c_{loss}^{pv} \left(\sum_{t=1}^T P_{loss,t}^{pv} - \sum_{t=1}^T 0.05 P_{pv,t} \right) \quad (29)$$

$$C_{ll} = \mu \cdot P_{loss,t} \Delta t \quad (30)$$

Style: C_g for the operating costs of thermal power units; C_{wpv} for scenery O&M costs; C_{loss} for the cost of lost load penalties; C_{ll} for the cost of wind and light abandonment; a, b, c The coefficients of the primary and secondary terms and the constant term for the cost of conventional thermal power units, respectively; e^{on}, e^{off} start-stop coefficients for conventional thermal power units, respectively; $D_{g,t}$ is the state component of a conventional thermal power unit startup and shutdown; $\lambda_{wind}, \lambda_{pv}$ for the number of wind power and photovoltaic O&M coefficients; $c_{loss}^{wind}, c_{loss}^{pv}$ is the penalty factor for wind and light abandonment; $P_{loss,t}^{wind}, P_{loss,t}^{pv}$ is the abandoned wind and light power in time period t ; $P_{wind,t}, P_{pv,t}$ is the maximum output power of wind power and photovoltaic in time period t ; μ is the lost load penalty factor.

4.2.2 Lower Level Model Constraints

(1) Power balance constraint [46]

$$P_{g,t} + P_{b,t}^{dis} - P_{b,t}^{ch} + P_{cx,t}^{dis} - P_{cx,t}^{ch} + P_{w,t} + P_{pv,t} + P_{loss,t} - P_{loss,t}^{wind} - P_{loss,t}^{pv} - P_{kk,t} - P_{load,t} = 0 \quad (31)$$

(2) Fire crew constraints [47]

$$P_g^{min} \leq P_{g,t} \leq P_g^{max} \quad (32)$$

$$-P_{g,p}^{min} \Delta t \leq P_{g,t} - P_{g,t-1} \leq P_{g,p}^{max} \Delta t \quad (33)$$

Style: P_g^{\max} , P_g^{\min} is the upper and lower output power limits for thermal power units, respectively; $P_{g,p}^{\max}$, $P_{g,p}^{\min}$ is upward and downward creep constraints for thermal units, respectively.

(3) Contact line power constraints [47]

$$0 \leq P_{line,t} \leq P_{line,\max} \quad (34)$$

Style: $P_{line,t}$ is the power of the contact line at time t ; $P_{line,\max}$ is the upper power limit of the contact line.

(4) Operational safety constraints [48]

$$\begin{cases} U_{i,\min} \leq U_{i,t} \leq U_{i,\max} \\ I_{ij,\min} \leq I_{ij,t} \leq I_{ij,\max} \end{cases} \quad (35)$$

Style: $U_{i,\max}$, $U_{i,\min}$ are the upper and lower limits of the voltage at node i ; $U_{i,t}$ is the voltage of node i at time period t ; $I_{ij,\max}$, $I_{ij,\min}$ are the maximum and minimum values of the branch ij allowed to flow current, respectively; $I_{ij,t}$ is the current flowing in branch ij at time t .

4.3 Construction of Flexibility Indicators for Regional Grids

The balance between supply and demand in a regional power grid is heavily influenced by the flexibility of various resources, including power-side, grid-measured, and load-side flexibility options. As flexibility demand fluctuates with changes in load, it is crucial to ensure that grid load activity stays within a specific flexibility regulation range to meet this demand effectively. This section assesses regional grid flexibility to evaluate whether flexibility resource issues are addressed and to measure their regulatory capabilities. It considers each resource's regulation capabilities, as detailed in the previous section, and introduces two key metrics: the flexibility dynamic range and the flexibility equilibrium degree.

4.3.1 Flexible Dynamic Range

This section highlights the dynamic range of flexibility inherent in the system, showcasing its adaptability. A higher upward flexibility value indicates the grid's enhanced capacity to handle uncertainties effectively. Conversely, a lower value suggests reduced reliability.

$$H_{fw} = \sum_{t=1}^T (P_t^{\text{up}} - P_t^{\text{down}}) \cdot R_t \quad (36)$$

$$R_t = (P_t^{\text{up}} - P_t^{\text{down}}) / P_{load,t} \quad (37)$$

$$\begin{cases} P_t^{\text{up}} = \sum_{i \in S_g} P_{g,i,t}^{\text{up}} + \sum_{i \in S_w} P_{w,j,t}^{\text{up}} + \sum_{i \in S_{pv}} P_{pv,k,t}^{\text{up}} + \sum_{i \in S_b} P_{b,h,t}^{\text{up}} - \sum_{i \in S_{cl}} P_{cl,m,t}^{\text{down}} \\ P_t^{\text{down}} = \sum_{i \in S_g} P_{g,i,t}^{\text{down}} + \sum_{i \in S_w} P_{w,j,t}^{\text{down}} + \sum_{i \in S_{pv}} P_{pv,k,t}^{\text{down}} + \sum_{i \in S_b} P_{b,h,t}^{\text{down}} - \sum_{i \in S_{cl}} P_{cl,m,t}^{\text{up}} \end{cases} \quad (38)$$

Style: H_{fw} Reflects the dynamic range of regional grid flexibility; P_t^{up} , P_t^{down} is an upper and lower limit for regional grid flexibility; R_t is the dynamic coefficient of flexibility at time t ; $P_{load,t}$ is the power of the load at time t .

This section evaluates the flexibility dynamic range by categorizing it into four grades—A, B, C, and D—based on various upward flexibility intervals. Refer to Table 1 for detailed classification and analysis.

Table 1: Flexibility dynamic range rating

Flexibility dynamic range rating	Upward flexibility interval
A	$P_t^{up} \geq 1.1P_{load,t}$
B	$1.1P_{load,t} > P_t^{up} \geq 1.05P_{load,t}$
C	$1.05P_{load,t} > P_t^{up} \geq P_{load,t}$
D	$P_{load,t} > P_t^{up}$

4.3.2 Flexibility and Balance

This paper introduces the concept of “grid flexibility balanced in time” to assess how effectively grid flexibility aligns with dispatch times in the power distribution network. As renewable energy sources increasingly penetrate the power grid, China has achieved a substantial total installed capacity of 58.69 GW in pumped storage power stations and 28,650 MW in electrochemical energy storage. Consequently, concerns about insufficient downward regulation capability are minimal during steady-state operations, particularly with the availability of controllable loads that enhance system operations. When it comes to grid flexibility, upward flexibility is more crucial than downward flexibility. Addressing downward flexibility can be managed by reducing reliance on wind and solar power and by utilizing energy storage charging. This paper, however, focuses exclusively on grid upward flexibility. The “flexibility balance degree” is a metric that indicates how evenly grid upward flexibility is distributed over time; a smaller value signifies a more balanced temporal distribution of this adjustment capability.

$$H_{bd} = \frac{1}{T} \sum_{t=1}^T |(P_t^{up} - P_{load,t} - H_{mod}) / H_{mod}| \quad (39)$$

$$H_{mod} = \frac{1}{T} \sum_{t=1}^T (P_t^{up} - P_{load,t}) \quad (40)$$

Style: H_{mod} is the average of the relative position of the load to the flexibility cap over the entire dispatch cycle; H_{bd} is the Flexibility Equilibrium Degree, which reflects the fluctuation of load across the flexibility range of the grid throughout the dispatch cycle.

To facilitate the measurement of the temporal equilibrium of flexibility resources, this subsection categorizes the flexibility equilibrium degree into four levels: A, B, C, and D, as shown in [Table 2](#). The reserve capacity of a regional power grid is typically set between 0.24 and 0.3. The reserve capacity requirement is still met when the flexibility equilibrium degree is 0.2. However, when the flexibility equilibrium degree reaches 0.8, it only marginally satisfies the spinning reserve demand. Based on these thresholds, the flexibility equilibrium degree is classified into the aforementioned four levels.

Table 2: Flexibility balance rating

Flexibility level of balance	Flexibility equilibrium range
A	$0.2 \geq H_{bd}$
B	$0.5 \geq H_{bd} > 0.2$
C	$0.8 \geq H_{bd} > 0.5$
D	$H_{bd} > 0.8$

Different scheduling strategies can significantly impact the flexibility curves of the grid, affecting both the upward and downward flexibility ranges. The upward flexibility range is calculated by subtracting the load curve from the upward flexibility curve. In contrast, the downward flexibility range is determined by subtracting the downward flexibility curve from the load curve. The hierarchical optimal dispatch strategy for new energy power systems, which factors in balanced grid flexibility responses, is detailed in the previous section. This strategy operates on a 15-min time frame, as illustrated in Fig. 5.

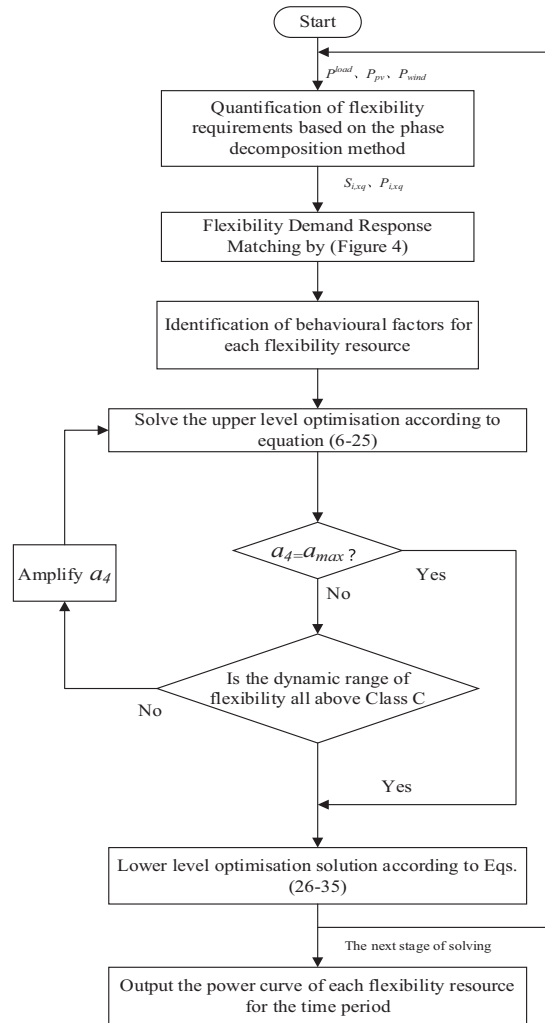


Figure 5: Optimising the control strategy process

5 Calculus Analysis

5.1 Introduction to Algorithmic System

In this study, we conducted an arithmetic analysis to evaluate the efficiency of the hierarchical optimal scheduling strategy for a new energy power system with an improved ratio. The system includes the following installed capacities: 900 MW of thermal power, 300 MW of wind power, 200 MW of photovoltaic (PV) power, 150 MW of pumped storage, and 30 MW of electrochemical storage. The setup comprises four thermal power units, one wind farm, one PV power plant, two pumped storage facilities, two energy storage stations, and a 20 MW controllable load. Thermal power serves as the foundation of the power system,

while pumped storage facilities, energy storage stations, and controllable loads significantly enhance system flexibility. Key parameters include a unit penalty for wind and solar curtailment set at 500 yuan/MWh, with a maximum allowable curtailment rate of 10%. A minor amount of load shedding is permissible. The electrochemical storage system features a charging and discharging efficiency of 95%, with maximum and minimum operational powers of 28 MWh and 2 MWh, respectively. The cost for charging and discharging is calculated at $[10,000 \text{ yuan} \cdot (\text{MW} \cdot \text{h})^{-1}] \times 0.002$. The total dispatch duration is configured for 6 h, with operations planned at 1-min intervals.

5.2 Optimised Scheduling Analysis

Traditional clustering algorithms require the input of the number of clusters, which leads to subjective interference in the clustering results; some algorithms randomly select the clustering center or search direction, which may lead to the clustering results falling into the local optimum [49]. AP clustering algorithms do not require human intervention in the whole process, so they are more objective. The new energy output curves of typical scenes are obtained through the AP clustering method, as shown in Fig. 6, and four typical scenes are clustered.

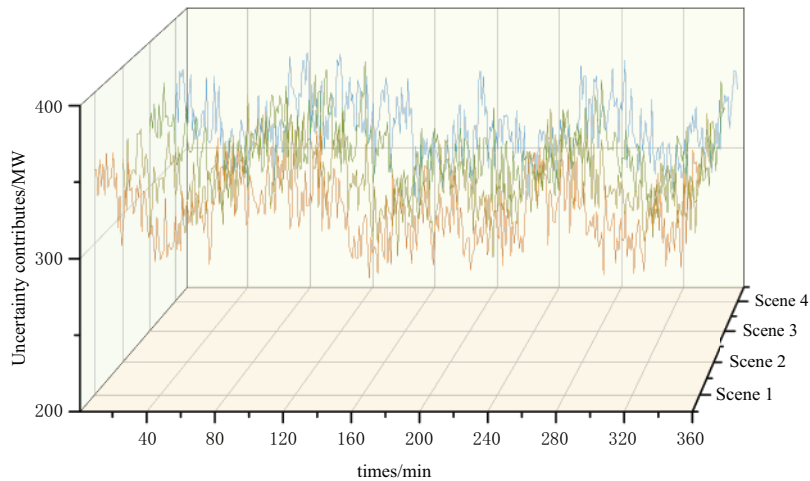


Figure 6: New energy uncertainty contributes

The additional operating cost for the conventional unit's upgraded model is calculated at \$91.2 million. Under Scene 2, the net load curves before and after optimal scheduling via the upgraded system are illustrated in Fig. 7. After implementing upper-tier pumped storage and energy storage optimization, the net load volatility difference under Scene 2 is reduced by 15.6%. During the 120–160 min and 240–310 min intervals, the net load reaches a trough period. Here, the optimized net load profile exceeds the pre-optimization levels as controllable loads are activated, and both pumped storage and energy storage systems are charged. This strategy improves operating revenue and minimizes net load fluctuations. In the 150–190 min period, when the net load peaks, previously accumulated surplus power from the pumped storage and energy storage is available to help shift the peak load effectively. This optimization process demonstrates that fluctuations in net load are reduced, helping to alleviate the strain on thermal power units and enhance the overall economic efficiency of system operations.

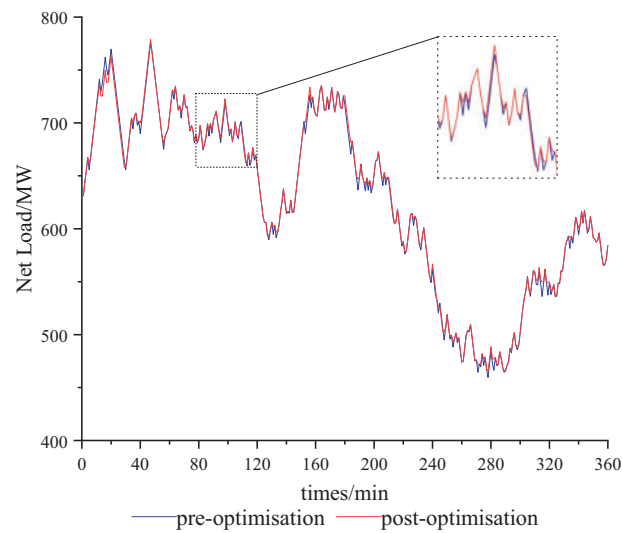


Figure 7: Net load profile before and after optimal scheduling in the lower upper tier of Scene 2

After the optimized scheduling of the upper and lower layers, the flexibility power curves under four typical Scenes with more extended periods are shown in Fig. 8, with a small amount of load loss occurring in Scene 1–4. The loss of load phenomenon occurs in the periods around 150 and 240 min, which fully uses the flexibility resources and enables the system to meet the flexibility dynamic requirements in 98.9% of the periods. Using two-tier optimal scheduling significantly improves the system's immunity to interference and reduces the lost load.

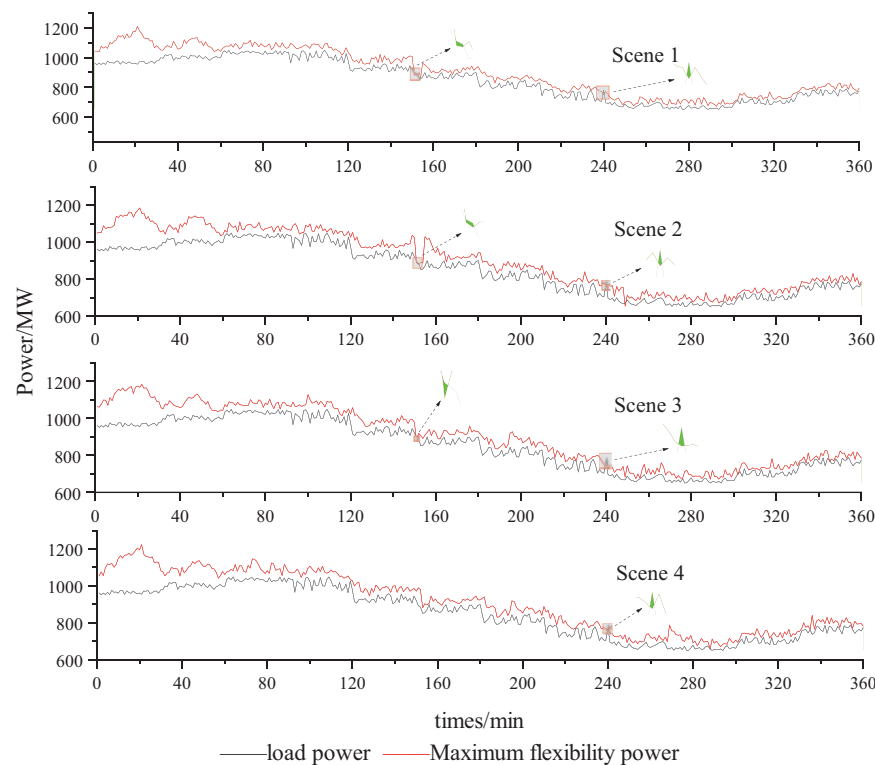


Figure 8: Maximum flexibility curve vs. load curve

The article compares the energy storage relative to the remaining power for the four Scenes, as shown in Fig. 9. Energy storage dispatch is categorized into three flexibility demand stages: high, medium, and low. During high flexibility demand, the relative residual power of energy storage across four Scenes ranges significantly from 0.42 to 0.92. Scene 3 experiences the most significant variation, while Scene 4 predominantly remains within 0.5 to 0.7, exhibiting minimal fluctuations. In this stage, energy storage is crucial in meeting peak demand, as thermal power and controllable loads fall short. In the medium flexibility demand stage, the residual power of energy storage varies slightly, from 0.2 to 0.42. Scene 2 shows the highest variability, whereas Scenes 3 and 4 typically range from 0.3 to 0.4. Here, energy storage demonstrates enhanced regulating capability. Finally, during low flexibility demand, the remaining power of storage across all Scenes is consistent, ranging from 0.1 to 0.2. The system becomes less dependent on storage for regulation, relying more on thermal power and controllable loads to manage peaks and optimize storage operation costs.

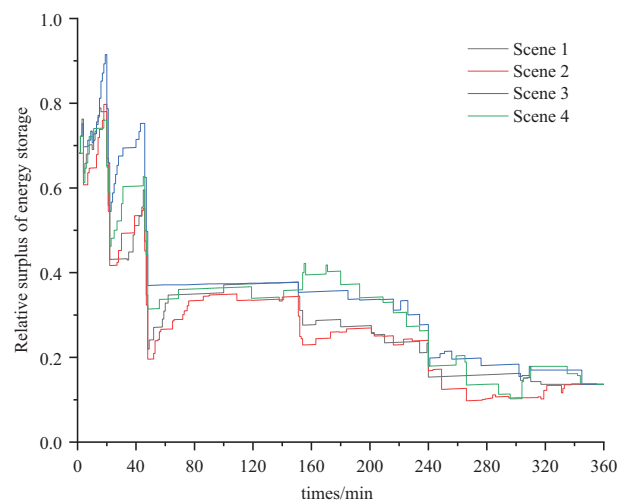


Figure 9: Comparison of the relative residual power of energy storage for 4 Scenes

5.3 Comparison of Optimal Scheduling Results under Different Scenarios

Translate the following content: In order to verify the effectiveness of this strategy, from the perspective of system operation economy and flexibility, to study the impact of the configuration of pumped storage power plants, controllable loads, and the consideration of flexibility balancing on the results of the optimal grid dispatch taking into account the flexibility of the adjustment capacity, the following Options are set up for case study analysis and comparison: Option 1, without the configuration of pumped storage power plants and controllable loads; Option 2, based on Option 1, considering Option 2, based on Option 1, considers the participation of pumped storage power plants in regulation and the participation of controllable loads in dispatch; Option 3, based on Option 1, considers the participation of pumped storage power plants in regulation and the overall flexibility of the regional grid; Option 4, based on Option 3, considers the participation of controllable loads in dispatch.

The generating unit outputs for the four Options are depicted in Fig. 10. In Option 1, thermal power units reach their limit in power output during the 5–60 min period, with a peak output of 890 MW. Only energy storage and thermal power units are used for peaking, leading to frequent high-frequency load losses and wind and solar energy abandonment. Option 2 introduces a pumped storage power plant, resulting in a 40 MW reduction in the minimum output and a 140 MW reduction in the maximum output of thermal power units compared to Option 1. This adjustment significantly diminishes the output fluctuations of

thermal power units. The pumped storage plant effectively participates in peak shifting from the 25th to the 50th minute, significantly reducing both the abandonment of wind and solar energy and the occurrence of load losses. In Option 3, controllable loads are added to Option 2's configuration. These loads bolster thermal power output between the 180th and 220th minutes, effectively curbing downward fluctuations. Their involvement enhances the system's operational revenue. Option 4 builds on Option 3 by aiming for superior grid flexibility regulation throughout the dispatch cycle. It achieves more balanced flexibility by adjusting the output of thermal power units: increasing output when flexibility is low and decreasing it when flexibility is high. This dynamic adjustment ensures optimal grid flexibility regulation.

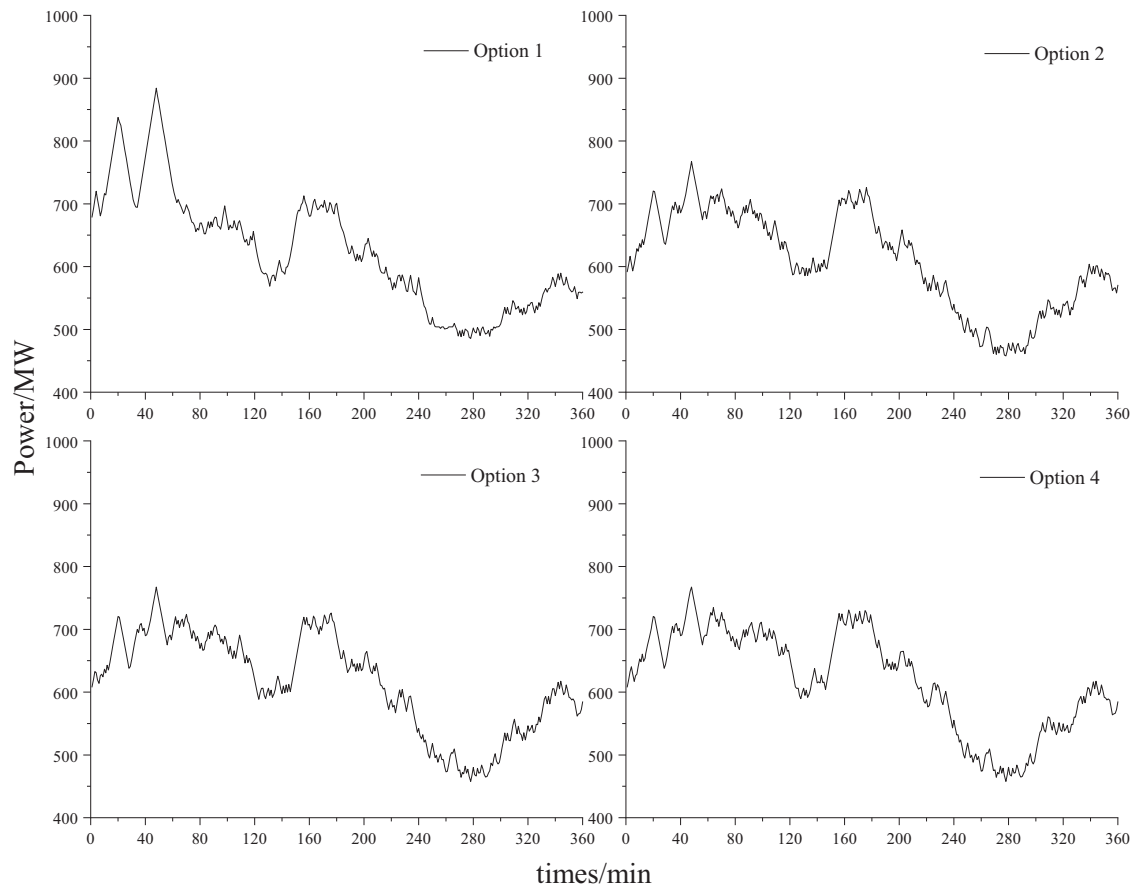


Figure 10: Output curves of thermal power units for 4 Options

Regarding grid flexibility, upward flexibility is more crucial than downward flexibility. Addressing downward flexibility can be managed by reducing reliance on wind and solar power and utilizing energy storage charging. In contrast, enhancing upward flexibility requires increasing the output capacity of flexible resources. To validate the effectiveness of the methodology presented in this study, we compared the upward flexibility of the grid across four different Options, as illustrated in Fig. 11. In Option 1, the upward flexibility curve, when compared to the load curve, reveals a slight load loss during the 200–240 min interval, indicating insufficient upward flexibility. Option 2 demonstrates a 15.2% enhancement in overall upward flexibility due to the integration of pumped storage. Although Option 3 does not show an increase in upward flexibility compared to Option 2 with the incorporation of controllable loads, it does reflect economic gains by maintaining system flexibility during the 50–180 min interval when controllable loads

are operational. Option 4 achieves an 11.3% gain in overall flexibility compared to Option 3, with reduced flexibility intervals (upward flexibility-load) between the 50–100 min and 200–250 min intervals. These findings underscore that our proposed strategy significantly improves the quality of the upward flexibility curve and its economic viability.

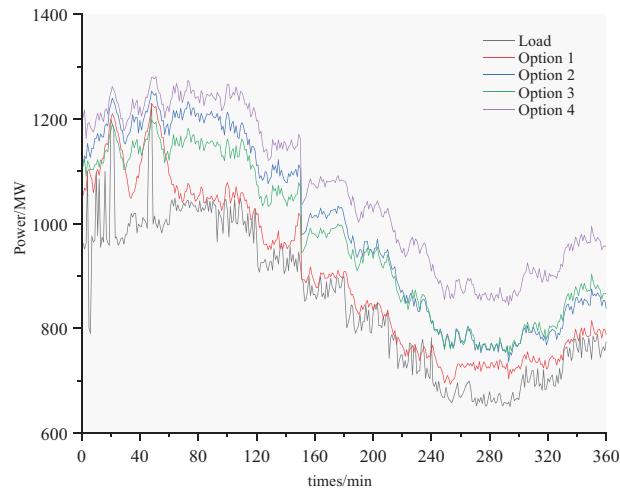


Figure 11: Grid upward flexibility comparison chart

To better understand system flexibility balancing, we introduced the concept of relative flexibility quantity. This measures the difference between upward flexibility and load during a specific period compared to the average difference over the dispatch cycle. This is visualized in Fig. 12. In Option 1, relative flexibility mostly exceeds two during the 0–50 min period but falls below zero between 200–240 min. This results in numerous lost load situations, signaling inadequate grid flexibility. Conversely, Option 2 achieves a maximum relative flexibility of 1.4 from 160–200 min, which is 0.1 and 0.13 higher than Options 3 and 4, respectively. This suggests that the flexibility resources are underutilized. During the 160–200 min period, Options 3 and 4 maintain relative flexibility between 0.8 and 1.2, meeting the A-level balance standard. Notably, Option 4 achieves this balance more optimally, maintaining the 0.8–1.2 range as early as 40 min into the cycle, demonstrating superior flexibility balance management.

In order to verify the effectiveness of the method proposed in this paper, an arithmetic analysis is carried out to compare the four proposed Options. As seen from Table 3, Option 2 reduces the operating cost by 29,550 RMB yuan compared with Option 1, effectively reduces wind and light abandonment, eliminates the loss of load, and improves a lot in terms of the degree of flexibility and balance. The total cost of Option 3 is reduced by 3380 RMB yuan after the addition of controllable loads, mainly relying on the benefits of controllable loads, and the degree of flexibility and balance is also improved. Compared to Option 3, the strategy in this paper increases the total cost by 90 RMB yuan but improves 62.8% in terms of grid flexibility, and the cost of wind and light abandonment is also reduced by 720 RMB yuan.

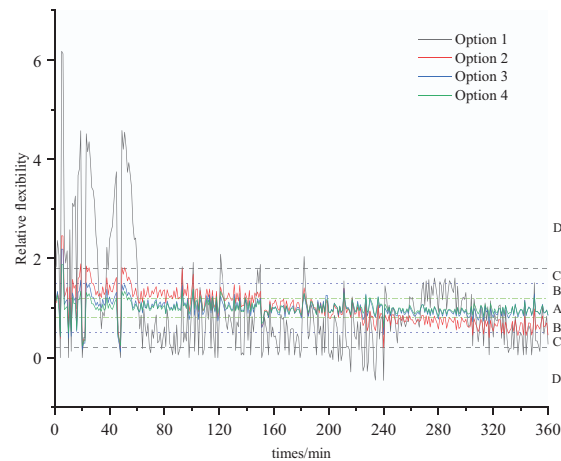


Figure 12: Relative flexibility comparison chart

Table 3: Comparison of system costs for Options 1–4

Option	Total costs (RMB)	Costs of wind and light abandonment (RMB)	Controllable load gain (RMB)	Load loss penalty (RMB)	Relative flexibility variance
1	998,560	1401	0	6420	384.194
2	969,010	645	0	0	44.192
3	965,630	512	4510	0	16.025
4	965,720	386	4230	460	9.842

6 Conclusions

This paper introduces a hierarchical optimal scheduling strategy to address the challenge of efficiently coordinating optimal scheduling in power systems to enhance the utilization of flexibility resources and maintain regional grid balance. This approach is designed for high proportions of new energy within power systems and focuses on achieving a balanced grid flexibility response. The key findings of the study are as follows:

- (1) The hierarchical optimal scheduling strategy aligns with actual peaking market rules, effectively leveraging the peaking capacity of energy storage and controllable loads. Compared to robust and economically optimal scheduling, it offers significant advantages regarding operational revenue and flexibility planning.
- (2) By quantifying system flexibility resources to determine its regulation capability, we can efficiently evaluate and plan flexibility demand responses. This approach ensures that flexibility demand is met while minimizing the iteration cycle.
- (3) Utilizing a two-layer optimization model enhances system output while maintaining safety. This model results in scheduling decisions that achieve optimal economic benefits and superior flexibility regulation capabilities.

This study has not conducted profound research on the downward regulation capability of flexibility. It has not done a good enough job regarding the economy while considering flexibility. Future research aims to improve the economics of scheduling by considering the factors of the electricity market in scheduling.

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Author Contributions: Cuiping Li: Conceptualization, Methodology, Writing—original draft. Jiacheng Sun: Methodology, Software, Writing—original draft. Qiang Li: Data curation, Formal analysis. Qi Guo: Investigation, Data curation. Junhui Li: Conceptualization, Methodology, Data curation, Formal analysis, Writing—review & editing. Shuo Yu: Data curation, Formal analysis. Jingbo Wang: Data curation, Methodology. Wenzhe Li: Data curation, Formal analysis. All authors reviewed the results and approved the final version of the manuscript.

Availability of Data and Materials: The data used to support the findings of this study are available from the corresponding author upon request.

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